

PRACTICE EXERCISES

Formulas: $\vec{p} = m\vec{v}$ $\vec{F}_{\text{net}} t = \Delta\vec{p}$ or $\vec{F}_{\text{net}} t = m\Delta\vec{v}$

1. Calculate the momentum of a 4.0 kg object travelling at a velocity of 12.0 m/s east.

$$\begin{aligned}\vec{p} &= m\vec{v} \\ &= (4)(12)[E] \\ &= \underline{48 \text{ kg}\cdot\text{m/s}} [E] \quad \checkmark\end{aligned}$$

2. A 5.0 kg object has momentum of 25.0 kg·m/s west. What is its velocity?

$$\vec{v} = \frac{\vec{p}}{m} = \frac{25 [W]}{5} = \underline{5.0 \frac{\text{m}}{\text{s}}} [W] \quad \checkmark$$

3. An object has a velocity of 8.0 m/s south and a momentum of 36.0 kg·m/s south. What is the mass of the object?

$$m = \frac{\vec{p}}{\vec{v}} = \frac{36 [S]}{8 [S]} = \underline{4.5 \text{ kg}} \quad \checkmark$$

4. An object has a velocity of 2.0 m/s east and momentum of 29 kg·m/s east. What is the magnitude of the weight of the object?

$$m = \frac{\vec{p}}{\vec{v}} = \frac{29 [E]}{2 [E]} = 14.5 \text{ kg} \leftarrow \text{mass}$$

$$F_g = (14.5)(9.81) = \underline{1.4 \times 10^2 \text{ N}} \quad \checkmark$$

5. A 6.6 N object is travelling at a velocity of 3.0 m/s north. What is the momentum of the object? (Express answer in kg·m/s.)

$$m = \frac{F}{a} = \frac{6.6}{9.81} = 0.67278 \text{ kg}$$

$$\vec{p} = m\vec{v} = (0.67278)(3 \text{ m/s} [N]) = \underline{2.0 \text{ kg}\cdot\text{m/s}} [N] \quad \checkmark$$

6. A 7.0 kg object travels 2.6 m west in 1.1 s. If velocity is uniform, what is the momentum of the object?

$$\vec{p} = m\vec{v} \quad \vec{v} = \frac{d}{t}$$

$$= (7 \text{ kg}) \left(\frac{2.6 \text{ m}}{1.1 \text{ s}} \right) [W] = 16.54 = \underline{17 \text{ kg m/s}} [W] \checkmark$$

7. A 5.0 kg object is dropped from a height of 2.5 m above the floor. What is the object's momentum after 0.25 s?

$$\vec{p} = m\vec{v}$$

$$= (5) (-2.4525)$$

$$= -12.2625 \text{ kg m/s}$$

$$= \underline{12 \text{ kg m/s}} [\text{down}] \checkmark$$

$$v_i = 0$$

$$v_f = ?$$

$$a = -9.81$$

$$t = 0.25$$

$$v_f = v_i + at$$

$$= (-9.81)(0.25)$$

$$= -2.4525 \text{ m/s}$$

8. An average net force of 17.0 N acts east on an object for 2.5×10^{-2} s. What is the impulse?

$$\text{impulse} = \vec{F}\Delta t$$

$$= (17 \text{ N})(2.5 \times 10^{-2} \text{ s})$$

$$= 0.425 = \underline{0.43 \text{ N}\cdot\text{s}} [E] \checkmark$$

9. An average net force of 11.2 N acts west on an object producing an impulse of 7.00 N·s west. How long did the force act on the object?

$$t = \frac{\text{imp}}{\vec{F}}$$

$$= \frac{7 \text{ N}\cdot\text{s} [W]}{11.2 \text{ N} [W]}$$

$$= \underline{0.625 \text{ s}} \checkmark$$

10. A 26.3 kg object is travelling at 21.0 m/s north. What average net force is required to bring this object to a stop in 2.60 s?

$$\text{imp} = \Delta p$$

$$F_{\text{net}} t = p_f - p_i$$

$$F_{\text{net}} = \frac{-mv}{t} = \frac{-(26.3)(21.0 \text{ m/s}) [N]}{2.6 \text{ s}} = -212 \text{ N}$$

$$= \underline{212 \text{ N}} [S] \checkmark$$

11. An average net force of 31.6 N south is used to accelerate a 15.0 kg object uniformly from rest to 10.0 m/s. How long was the acceleration?

$$\begin{aligned}\vec{imp} &= \Delta \vec{p} \\ \vec{F}_{net} t &= \vec{p}_f - \vec{p}_i \\ t &= \frac{\vec{p}_f}{\vec{F}} = \frac{m\vec{v}}{\vec{F}} = \frac{(15)(10)}{31.6} = 4.75 \text{ s} \quad \checkmark\end{aligned}$$

12. An average net force of 25.0 N acts north on an object for 7.20×10^{-1} s. What is the change in momentum of the object?

$$\begin{aligned}\Delta \vec{p} &= \vec{imp} \\ &= \vec{F} \Delta t \\ &= (25 \text{ N})(7.2 \times 10^{-1}) \\ &= 18.0 \text{ kg m/s [N]} \quad \checkmark\end{aligned}$$

13. A 5.00 kg object accelerates uniformly from rest to a velocity of 15.0 m/s east. What is the impulse on the object?

$$\begin{aligned}\vec{imp} &= \Delta \vec{p} = \vec{p}_f - \vec{p}_i \\ &= m\vec{v}_f - m\vec{v}_i \\ &= (5)(15) = 75 \text{ N}\cdot\text{s [E]} \quad \checkmark\end{aligned}$$

14. An average net force caused an 11.0 kg object to accelerate uniformly from rest. If this object travels 26.3 m west in 3.20 s, what is the change in momentum of the object?

$$\begin{aligned}\Delta \vec{p} &= \vec{p}_f - \vec{p}_i \\ &= m\vec{v}_f \\ &= (11 \text{ kg})(16.4375 \text{ m/s}) \\ &= 181 \text{ kg m/s [West]} \quad \checkmark\end{aligned}$$

$\vec{p}_i = 0$
 $v_f = ?$
 $t = 3.2$
 $d = 26.3 \text{ [W]}$
 $v_i = 0$
 $d = v_{avg} t$
 $= \left(\frac{v_f - v_i}{2} \right) t$
 $v_f = \frac{2d}{t} = \frac{2(26.3)}{3.2} = 16.4375$

15. A 3.0 kg object is dropped from a height of 6.5 m. How far has the object fallen when its momentum is 6.0 kg·m/s down?

$$\begin{aligned}\Delta \vec{p} &= \vec{p}_f - \vec{p}_i \\ &= m\vec{v}_f \\ v_f &= \frac{\Delta \vec{p}}{m} \\ &= \frac{6}{3} = 2 \text{ m/s [down]}\end{aligned}$$

$d = ?$
 $v_f = -2 \text{ m/s}$
 $a = -9.81 \text{ m/s}^2$
 $v_i = 0$
 $v_f^2 = 0 + 2ad$
 $(-2)^2 = 2(-9.81)d$
 $d = -0.203 \text{ m}$
 $= 0.20 \text{ m [down]} \quad \checkmark$

16. A 1.0 kg ball hits the floor with a velocity of 2.0 m/s. If this ball bounces up with a velocity of 1.6 m/s, what is the ball's change in momentum?

$$\begin{aligned}\Delta \vec{p} &= \vec{p}_f - \vec{p}_i \\ &= m\vec{v}_f - m\vec{v}_i \\ &= (1\text{ kg})(1.6\text{ m/s up}) + (1\text{ kg})(2\text{ m/s down}) \\ &= \underline{3.6\text{ kg m/s [up]}} \quad \checkmark\end{aligned}$$

17. A rocket at rest with a mass of 9.5×10^3 kg, is acted on by an average net force of 1.5×10^5 N up for 15 s. What is the final velocity of the rocket?

$$\begin{aligned}\vec{p}_f &= \vec{F}\Delta t = \Delta \vec{p} = \vec{p}_f - \vec{p}_i^0 \\ \vec{F}\Delta t &= m\vec{v}_f \\ (1.5 \times 10^5 \text{ N up})(15 \text{ s}) &= 9.5 \times 10^3 \text{ kg } \vec{v}_f \\ v_f &= \underline{2.4 \times 10^2 \text{ m/s [up]}} \quad \checkmark\end{aligned}$$

18. Without finding the acceleration, calculate the average net force that is required to accelerate a 5.4 kg ball from rest to 3.0 m/s east in a time of 0.75 s.

$$\begin{aligned}\vec{F}\Delta t &= \vec{p}_f - \vec{p}_i^0 \\ F &= \frac{\vec{p}_f}{\Delta t} = \frac{m\vec{v}_f}{t} \\ &= \frac{(5.4\text{ kg})(3\text{ m/s [E]})}{0.75\text{ s}} = 21.6 = \underline{22\text{ N [E]}} \quad \checkmark\end{aligned}$$

19. Without finding the acceleration, calculate the time an average net force of 225 N must act on a 1.0×10^3 kg object to change its velocity from 2.0 m/s east to 5.0 m/s east.

$$\begin{aligned}\vec{F}\Delta t &= \vec{p}_f - \vec{p}_i \\ t &= \frac{m\vec{v}_f - m\vec{v}_i}{F} \\ t &= \frac{(1000)(5\text{ [E]}) - 1000(2\text{ [E]})}{225\text{ N}} = \underline{13\text{ s}} \quad \checkmark\end{aligned}$$

20. Without finding the acceleration, calculate the change in velocity of a 15 kg object when an average net force of 95 N north acts on the object for 1.6 s.

$$\begin{aligned}\vec{F}\Delta t &= m\Delta \vec{v} \\ \Delta \vec{v} &= \frac{\vec{F}\Delta t}{m} \\ &= \frac{(95\text{ N North})(1.6\text{ s})}{15\text{ kg}} = \underline{10\text{ m/s [North]}} \quad \checkmark\end{aligned}$$