More Trigonometry Problems

Name: _____Key_____

Date: _____ Block:_____

Show your work and draw a diagram for each question

1. When the foot of a ladder is 2 m from a wall, the angle formed by the ladder and the ground is 68°. How high up the wall does the ladder reach?
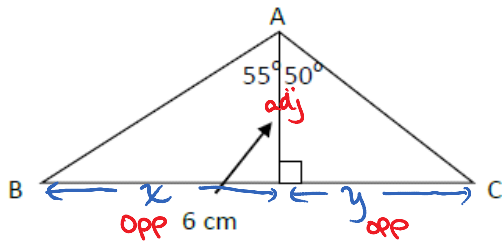
$$\tan 68° = \frac{h}{2}$$

$$2\tan 68° = h$$

$$\boxed{h = 5.0m}$$

h
opp
68°
2m
adj
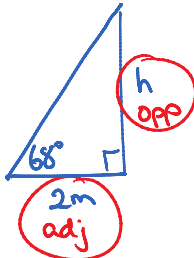
2. Calculate the length of BC to 1 decimal place.

A
55° 50°
adj
B
opp   6 cm
x   y
opp
C

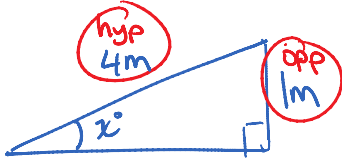$$\tan 55° = \frac{x}{6}$$

$$6\tan 55° = x$$

$$x = 8.5688...$$

$$\tan 50° = \frac{y}{6}$$

$$6\tan 50° = y$$

$$y = 7.1505...$$

$$BC = x + y = 8.5688... + 7.1505... = \boxed{15.7cm}$$

3. The roof of a house rises 1 m for every 4 m along its surface. Determine the angle of elevation of the roof, to the nearest tenth of a degree.

hyp
4m
opp
1m
x°

$$\sin x° = \frac{1}{4}$$

$$x° = \sin^{-1}\left(\frac{1}{4}\right)$$

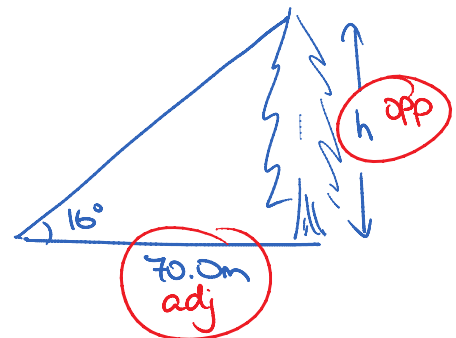$$\boxed{x° = 14.5°}$$

4. From a horizontal distance of 70.0 m, the angle of elevation to the top of a tree is 16°. Calculate the height of the tree to the nearest tenth of a metre.

$$\tan 16° = \frac{h}{70.0}$$

$$70.0\tan 16° = h$$

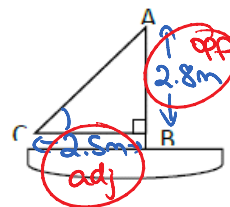$$\boxed{h = 20.1m}$$

16°
70.0m
adj
h opp

5. The mast *AB* is 2.8 m long and the boom *BC* is 2.5 m long on the sailboat pictured. Determine $\angle C$ to one decimal place.
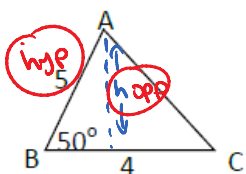
$$\tan C = \frac{2.8}{2.5}$$

$$\angle C = \tan^{-1}\left(\frac{2.8}{2.5}\right)$$

$$\boxed{\angle C = 48°}$$

6. Calculate the area of $\triangle ABC$ to the nearest hundredth.

$$A = \frac{bh}{2} \quad \rightarrow \text{ need } h \text{ first}$$

$$\sin 50° = \frac{h}{5}$$

$$5\sin 50° = h$$

$$h = 3.8302...$$

$$A = \frac{bh}{2}$$

$$A = \frac{(4)(3.8302...)}{2}$$
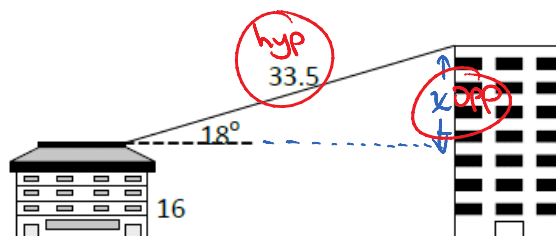
$$\boxed{A = 7.66 \text{ units}^2}$$

7. A tightrope water attaches a cable to the roofs of two adjacent buildings as shown. The cable is 33.5 m long. The angle of elevation of the cable is 18°. The shorter building is 16.0 m high. What is the height of the taller building, to 1 decimal place?

$$\sin 18° = \frac{x}{33.5}$$

$$33.5\sin 18° = x$$

$$x = 10.3520...$$

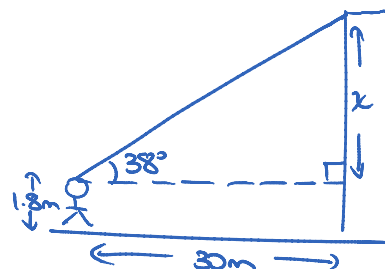$$\text{taller building} = 10.3520... + 16$$

$$= \boxed{26.4m}$$

8. Jimmy is standing 30 m away from a building and looks with an angle of elevation of 38° to the top of the building. If Jimmy is 1.8 tall, how tall is the building? Draw a diagram, and round your answer to 1 decimal place.

$$\tan 38° = \frac{x}{30}$$

$$30\tan 38° = x$$

$$x = 23.4385...$$

$$\text{height} = 23.4385... + 1.8$$

$$= \boxed{25.2m}$$

9. A large tree is to be transported to a new location. The tree is held vertical by means of two guy wires of unequal length on opposite sides of the tree. One of the wires makes an angle of 48° with the ground. The other wire is 12 m long and makes an angle of 56° with the ground. Both wires are attached 3 m down from the top of the tree.

    a) Draw a diagram to illustrate the scenario

    3m $\updownarrow$ 12m   48°   56° x
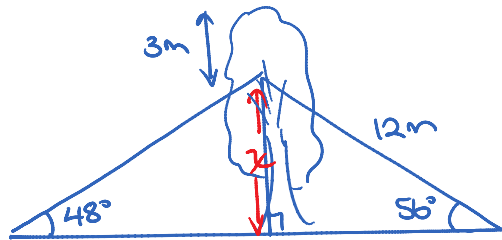
    b) Determine the height of the tree to one decimal place

    3m   12m x 56°
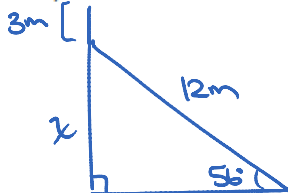
    $$\sin 56° = \frac{x}{12}$$
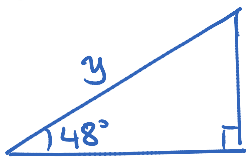
    $$12\sin 56° = x$$

    $$x = 9.9484...$$

    height = 9.9484... + 3

    = $\boxed{12.9m}$

    c) Determine the length of the other wire to the nearest tenth of a metre

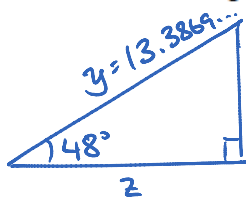 y $x = 9.9484...$ 48°

    $$\sin 48° = \frac{9.9484...}{y}$$

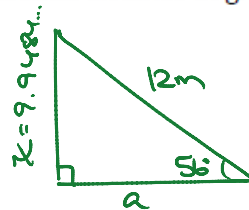 $$y = \frac{9.9484...}{\sin 48°}$$

    $$y = 13.3869...$$ → $\boxed{y = 13.4m}$

    d) Determine to the nearest tenth of a metre, the horizontal distance at ground level between the two guy wires

    $y = 13.3869...$ $x = 9.9484...$ 48° z

    $$(9.9484...)^2 + z^2 = (13.3869...)^2$$

    $$z^2 = 80.2390...$$

    $$z = 8.9576...$$

    $x = 9.9484...$ 12m   56° a

    $$(9.9484...)^2 + a^2 = 12^2$$

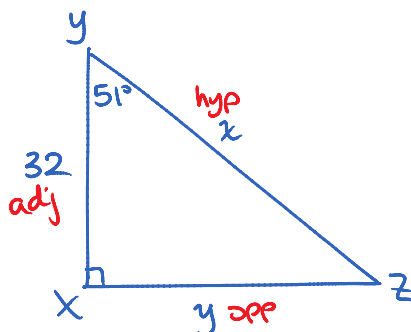 $$98.9716... + a^2 = 144$$

    $$a^2 = 45.0283...$$

    $$a = 6.7103...$$

    total horiz. dist = $z + a$ = $\boxed{15.7m}$

10. Solve $\triangle XYZ$, given $\angle X = 90°$, $XY = 32$ and $\angle Y = 51°$. Round answers to 1 decimal place.

    y 51°   hyp x 32 adj X y opp z

    Find x

    $$\cos 51° = \frac{32}{x}$$

    $$x = \frac{32}{\cos 51°}$$

    $$\boxed{x = 50.8}$$

    Find y

    $$\tan 51° = \frac{y}{32}$$

    $$32\tan 51° = y$$

    $$\boxed{y = 39.5}$$

    $$\angle Z = 180° - 90° - 51°$$

    $$\boxed{\angle Z = 39°}$$

11. Danny and Elaine are standing at points D and E respectively. The angles of elevation to a treetop at point T are as shown. If the tree is 50 m tall, how far apart are Danny and Elaine, to the nearest tenth of a metre?
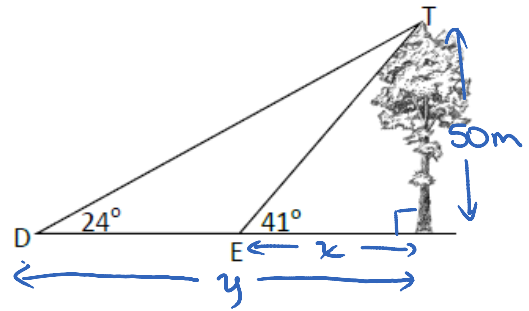
Find x

$$\tan 41° = \frac{50}{x}$$

$$x = \frac{50}{\tan 41°}$$

$$x = 57.5184\ldots$$

Find y

$$\tan 24° = \frac{50}{y}$$

$$y = \frac{50}{\tan 24°}$$

$$y = 112.3018\ldots$$

① Distance $DE = y - x = 112.3018\ldots - 57.5184\ldots$

$$= 54.7834\ldots$$

$$= \boxed{54.8 \text{ m}}$$