

Exponents #3 - Integral Exponents

Sep 17

Notice the pattern! If you know the positive value, then you have a hint for the negative power

$$\begin{array}{l}
 3^4 = 81 \\
 3^3 = 27 \\
 3^2 = 9 \\
 3^1 = 3 \\
 3^0 = 1 \\
 3^{-1} = \frac{1}{3} \\
 3^{-2} = \frac{1}{9} \\
 3^{-3} = \frac{1}{27} \\
 3^{-4} = \frac{1}{81}
 \end{array}$$

$\div 3$ which is the same as $\frac{81}{3}$
 $\div 3 = \frac{27}{3}$
 $\div 3 = \frac{9}{3}$
 $\div 3$

9 and $\frac{1}{9}$ are reciprocals... So 3^2 and 3^{-2} are reciprocals.

Ex. $6^{-2} = ?$ So $6^2 = 36$ so 6^{-2} is $\frac{1}{36}$ (reciprocal of 36)

Ex. $\frac{1}{4^{-3}} = ?$ Means $1 \div 4^{-3} = 1 \div \frac{1}{4^3} = 1 \times \frac{4^3}{1} = 4^3$

multiply by the reciprocal (dividing fractions)
 reciprocal $\rightarrow 4^3$

So: $\frac{1}{4^{-3}} = \frac{4^3}{1}$

When a power is moved from one place (top or bottom) to the other in a fraction, the exponent changes to its opposite.

★ Positive exponents are easier to work with!

Ex. $\frac{2^{-3}}{5^{-2}} = \frac{5^2}{2^3} = \frac{25}{8}$

or $2^{-3} \div 5^{-2} = \frac{1}{8} \div \frac{1}{25} = \frac{1}{8} \times \frac{25}{1} = \frac{25}{8}$

Ex. $\frac{4a^{-3}}{b^2} = \frac{4}{b^2 \cdot a^3}$

every number has an exponent (only powers with negative exponents have to move)

The most important idea from today's lesson is :

Sep 18

Ex $2x^{-3}$ is really $2^1 x^{-3}$

use Integral exponent law to remove negative

$$\frac{2^1}{x^3}$$

$$\frac{2}{x^3}$$

Ex $(2x)^{-3}$

use Power of Product to remove brackets

$$2^{-3} x^{-3}$$

use the Integral exponent law to remove negatives on exponents

$$\frac{1}{2^3 x^3}$$

$$\frac{1}{8x^3}$$

evaluate coefficient

Ex

$$\frac{5(x^3 y^4)^{-1}}{(3x^{-2} y^6)^{-2}}$$

Power of a Product law

$$\frac{5(x^{-3} y^{-4})}{3^{-2} \cdot x^4 y^{-12}}$$

Integral exponent law

$$\frac{5 \cdot 3^2 \cdot y^{12}}{x^3 \cdot y^4 \cdot x^4}$$

Mult. law & division law of exponents

$$\frac{45 \cdot y^8}{x^7} \text{ is the same as } 45 \frac{y^8}{x^7}$$

Always use
HAPPY
exponents

